

# Autograding Weakest Precondition Proofs and Dafny Specifications

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# CSSE3100/7100 Reasoning about Programs

|                               |           |      |     |
|-------------------------------|-----------|------|-----|
| • Introduction                | (1 week)  |      |     |
| • Weakest precondition proofs | (3 weeks) |      |     |
| • Dafny methods               | (4 weeks) |      |     |
| • pre/postconditions          |           | 2018 | 73  |
| • loop invariants / variants  |           | ↓    |     |
| • Dafny classes               | (3 weeks) | 2025 | 217 |
| • data abstraction            |           |      |     |
| • Other topics                | (1 week)  |      |     |

3<sup>rd</sup>-year undergraduate and Masters

Number of students

# CSSE3100/7100 Reasoning about Programs

- Introduction (1 week)
- Weakest precondition proofs (3 weeks) ← Assignment 1
- Dafny methods (4 weeks) ← Assignment 2
  - pre/postconditions
  - loop invariants / variants
- Dafny classes (3 weeks) ← Assignment 3
  - data abstraction
- Other topics (1 week)

# Requirements for the autograder

1. Allow fine-grained marking
  - part marks for partially correct solutions
2. Not artificially constrain students' use of programming techniques \*
  - allow them to apply best programming practices
3. Be reusable for new versions of assignments
  - with minimal input from teaching staff

\* Unless there is a pedagogical reason

# Proofs in Dafny

```
method M(s: nat, t: nat) returns (r: nat)
  requires s > 0 && t > 1
  ensures r < s
{
  r := s/t;
}
```

postcondition could not be proved

# Proofs in Dafny

```
method M(s: nat, t: nat) returns (r: nat)
  requires s > 0 && t > 1
  ensures r < s
{
  { s/t < s }
  r := s/t;
  { r < s }
}
```

postcondition could not be proved

# Proofs in Dafny

```
method M(s: nat, t: nat) returns (r: nat)
  requires s > 0 && t > 1
  ensures r < s
{
  { s/t < s }
  r := s/t;
  { r < s }
}
```

postcondition could not be proved

```
method M(s: nat, t: nat) returns (r: nat)
  requires s > 0 && t > 1
  ensures r < s
{
  calc {
    s/t < s;
    == (s/s)/t < s/s;
    == 1/t < 1;
  }
  r := s/t;
}
```

# Assignment 1 – weakest precondition proofs

```
...
while n != 33
  invariant s == n*(n-1)/2
{
  { s == n*(n-1)/2 && n != 33 }           (strengthening)
  { s == n*(n-1)/2 }                     (arithmetic)
  { s + n == n*(n-1)/2 + n }
  s := s + n;
  { s == n*(n-1)/2 + n }
  ...
}
...
```

# Assignment 1 – weakest precondition proofs

```
...
while n != 33
  invariant s == n*(n-1)/2
{
  ghost var WP: bool, WP_s: bool;
  WP_s := s == n*(n-1)/2 && n != 33; // strengthening
  WP := s == n*(n-1)/2;             // arithmetic
  WP := s + n == n*(n-1)/2 + n;
  s := s + n;
  WP := s == n*(n-1)/2 + n;
  ...
}
...
```

# Assignment 1 – Checker file

```
... // supporting functions
```

```
class Checker {  
    var v // input, output and local variables  
    ... // checking method goes here  
}
```

```
Equivalence      WP :=  $\phi$ ;  
                  WP :=  $\psi$ ;
```

```
method Check() {  
    assume  $\alpha$ ; //  $\alpha$  is teaching-staff provided assumptions  
    calc {  $\phi$ ; ==  $\psi$ ; }  
}
```

Also, while and if-else conditions, e.g.,

```
WP :=  $\phi$ ;  
if B {WP := P; ...} else {WP := Q; ...}  
  
calc { $\phi$ ; == ((B ==> P) && (!B ==> Q));}
```

# Assignment 1 – Checker file

... // supporting functions

```
class Checker {  
  var v // input, output and local variables  
  ... // checking method goes here  
}
```

Strengthening       $WP\_s := \phi;$   
                          $WP := \psi;$

```
method Check() {  
  assume  $\alpha;$   
  calc {  $\phi; ==> \psi;$  }  
}
```

```
method Check() {  
  assume  $\alpha;$   
  calc {  $\psi; ==> \phi;$  }      // should fail  
}
```

# Assignment 1 – Checker file

```
WP :=  $\phi$ ;  
x := E;  
WP :=  $\psi$ ;
```

```
method Check()  
  modifies this  
{  
  assume  $\alpha$ ;  
  x := E;  
  assert  $\psi \iff \text{old}(\phi)$ ;  
}
```

Proof:

```
{ $\psi[x \setminus E] \iff \phi$ }      (at start of method)  
{ $\psi[x \setminus E] \iff \text{old}(\phi)$ } (old values are constant)  
x := E;  
{ $\psi \iff \text{old}(\phi)$ }      (wp(assert P, Q) = P && Q)  
assert  $\psi \iff \text{old}(\phi)$ ;  
{true}                    (no explicit postcondition)
```

# Assignment 2 – Specifying and implementing Dafny methods

Specification compared against teaching-staff provided solution

- i. Full student pre or postcondition must imply each conjunct of the solution (not too weak)
- ii. The full solution implies each of the conjuncts of the student pre or postcondition (not too strong)
- iii. The full student pre or postcondition is not false!

## Assignment 2 – Checking preconditions

... // supporting functions (from assignment)

... // additional functions (from student)

```
class Checker {  
    ... // checking methods go here  
}
```

### Preconditions

```
method Check( $v_{in}$ ) {  
    assume  $\alpha$ ;  
    calc {  $\Psi$ ; ==> false; }  
} // should fail
```

```
method Check( $v_{in}$ ) {  
    assume {:axiom}  $\alpha$ ;  
    calc {  $\Psi$ ; ==>  $\phi_i$ ; }  
}
```

```
method Check( $v_{in}$ ) {  
    assume {:axiom}  $\alpha$ ;  
    calc {  $\Phi$ ; ==>  $\psi_i$ ; }  
}
```

$\Psi$  is student precondition,  $\psi_i$  is its i-th conjunct

$\Phi$  is solution precondition,  $\phi_i$  is its i-th conjunct

# Assignment 2 – Checking postconditions

## Postconditions

```
method Change( $v_{in}$ )  
  modifies  $\delta$ 
```

```
method Check( $v$ )  
  modifies  $\delta$   
{  
  assume  $pre$ ;  
  Change( $\mu_{in}$ );  
  assume  $\alpha$ ;  
  calc {  $\Psi$ ;  $\implies$  false; }  
} // should fail
```

```
method Change( $v_{in}$ )  
  modifies  $\delta$ 
```

```
method Check( $v$ )  
  modifies  $\delta$   
{  
  assume { :axiom }  $pre$ ;  
  Change( $\mu_{in}$ );  
  assume { :axiom }  $\alpha$ ;  
  calc {  $\Psi$ ;  $\implies$   $\phi_i$ ; }  
}
```

```
method Change( $v_{in}$ )  
  modifies  $\delta$ 
```

```
method Check( $v$ )  
  modifies  $\delta$   
{  
  assume { :axiom }  $pre$ ;  
  Change( $\mu_{in}$ );  
  assume { :axiom }  $\alpha$ ;  
  calc {  $\Phi$ ;  $\implies$   $\psi_i$ ; }  
}
```

$\Psi$  is student postcondition,  $\psi_i$  is its  $i$ -th conjunct  
 $\Phi$  is solution postcondition,  $\phi_i$  is its  $i$ -th conjunct

## Assignment 2 – Checking invariants

- See if the student's code verifies for each correct conjunct of the student's postcondition
  - verification succeeds if they have an invariant which ensures that postcondition

// additional methods and lemmas (from student)

method Check( $v_{in}$ ) returns ( $v_{out}$ )

requires  $pre$

modifies  $\delta$

ensures  $\psi_{ensi}$

{

*code*;

}

No assumptions included, student's must ensure their code verifies

# Evaluation

1. By how much is manual marking time reduced?

| Year | Assignment 1 | Assignment 2 |
|------|--------------|--------------|
| 2024 | 20.08        | 21.92        |
| 2025 | 9.87 (50%)   | 5.05 (77%)   |

Mean manual marking time (minutes per submission)

2. By how much is marking accuracy increased?

| Year | Assignment 1 | Assignment 2 |
|------|--------------|--------------|
| 2024 | 22%          | 44%          |
| 2025 | 11%          | 29%          |

Number of re-mark requests resulting in changes to marks

# Conclusion

Dafny autograder for

- fine-grained marking of wp proofs, pre/post specifications and invariants
- allow maximum flexibility in writing code
- easy to reuse for new assignments

Extended for a third assignment using Dafny classes for data structures

Successfully trialled on ~380 students in 2025 and 2026

Future directions: tutoring system for feedback to short-answer questions